# 24. Molecular Polarisability. The Anisotropy of the $\mathrm{H}-\mathrm{O}$ Bond in Normal Alcohols. 

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#### Abstract

Measurements of the molar Kerr constants of 14 n -alcohols between methanol and octadecanol are reported. Semi-axes of the polarisability ellipsoids for the first six alcohols are calculated and discussed. From methyl alcohol the longitudinal and transverse polarisabilities of the $\mathrm{O}-\mathrm{H}$ bond appear as $0.09_{5}$ and $0.05 \times 10^{-23}$ c.c. Such values are used to indicate that the preferred conformation of ethyl alcohol is s-trans. Approximate constant differences between corresponding semi-axes of adjacent homologues are noted and interpreted as due to a common pattern of configuration throughout the series.


This paper records measurements of the molar Kerr constants $\infty\left({ }_{m} K_{2}\right)$ of fourteen normal alcohols at infinite dilution in carbon tetrachloride; it proceeds inter alia to an estimate of the semi-axes of the polarisability ellipsoid of the $\mathrm{H}-\mathrm{O}$ bond, and thence to a consideration of the configurations apparently adopted by the solutes in this medium.

Practical procedures, details regarding calculations, definitions of symbols, etc., follow those of ref. 1. Actual observations of the changes of electric double refraction and refractive index ( Na light), caused in carbon tetrachloride by the presence of a weight fraction $w_{2}$ of solute, are listed in Table 1, and lead to the coefficients in Table 2. Table 3 gives the values of $\infty\left({ }_{m} K_{2}\right)$ derivable with the help of the appropriate dielectric constant and density factors ( $\alpha \varepsilon_{1}$ and $\beta$ respectively) from Le Fèvre and Williams. ${ }^{2}$ The availability ${ }^{3}$ of the quantities $\infty_{\infty} \delta_{2}{ }^{2}$ for the alcohols from methyl to hexyl now makes possible the estimation of " apparent" molecular semi-axes of polarisability for these six substances; " apparent" because, throughout the calculations, the assumption is made that $\mu_{\text {resultant }}$ is always acting parallel to one of the principal axes of the ellipsoid concerned. Results are summaried as Table 4, in which the electronic polarisations ${ }_{\mathrm{II}} P$ are extrapolated from the molecular refractions recorded for the $C$ and $G^{\prime}$ lines by Vogel, ${ }^{4}$ and the dipole moments are from ref. 2.

Previous Electric Double Refraction Data for Alcohols.-The Kerr constants, expressed relatively to $B_{\mathrm{CS}_{2}}$, of a number of pure alcohols are listed in the International Critical Tables, Vol. VII. Except for ethyl alcohol, they are all markedly negative. Where solutions are concerned, the only earlier work appears to be that by Tsvetkov and Marinen ${ }^{5}$ who reported molar Kerr constants for ten of the solutes now studied by us. These authors state that their ${ }_{m} K$ 's were drawn from alcohol-benzene mixtures, but no experimental details were given. The ${ }_{\infty}\left(\mathrm{m}_{\mathrm{m}} K_{2}\right)$ 's of Table 3 vary between being about $\frac{1}{2}$ and $\frac{1}{9}$ of the ${ }_{m} K$ 's claimed by the Russians. The discrepancies are far too great to arise solely from " solvent effects"; their possible origins will be discussed in the following paper. Stuart and Volkmann ${ }^{6}$ examined the vapours of methyl and ethyl alcohol in 1933 with indefinite results, quoting $K=B \lambda / n$ (where $B=$ Kerr constant, $\lambda=$ wavelength in vacuo of light used, $n=$ refractive index of field-free medium) at 760 mm . pressure as $\pm 0.4 \times 10^{-15}$ and $\pm 0.5 \times 10^{-15}$ respectively for temperatures of $98.8^{\circ}$ and $102^{\circ}$.

## Discussion

Three main points of interest which arise from these results are (a) whether or not a reliable estimate of the anistropy of polarisability of the $\mathrm{O}-\mathrm{H}$ bond can be derived, (b)
${ }^{1}$ Le Fèvre and Le Fèvre, Rev. Pure Appl. Chem., 1955. 5, 261; J., 1953, 4041; 1954, 1577.
${ }^{2}$ Le Fèvre and Williams, $J$., 1960, 108.
${ }^{3}$ Le Fèvre and Rao, J., 1960, 119.
${ }^{4}$ Vogel, $J$., 1948, 1814.
${ }_{5}$ Tsvetkov and Marinen, Doklady Akad. Nauk., S.S.S.R., 1948, 62, 67; Chem. Abs., 1949, 48, 469.
${ }^{6}$ Stuart and Volkmann, Ann. Phys., 1933, 18, 121.

Table 1. Kerr effects and refractive indexes for solutions of alcohols in carbon tetrachloride at $25^{\circ}$.


TABLE 2. Coefficients a and b in equations $10^{7} \Delta \mathrm{~B}=\mathrm{aw}_{2}+\mathrm{bw}_{2}{ }^{2}$, also values of the quotients $\Sigma \Delta \mathrm{n} / \Sigma \mathrm{w}_{2}$.

| Solute alcohol | $a$ | $b$ | $\Sigma \Delta n / \Sigma w_{2}$ | Solute alcohol | $a$ | $b$ | $\Sigma \Delta n / \Sigma w_{2}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Methyl | $-0.088{ }_{0}$ | $+48.2$ | -0.240 | Nonyl | $-0.392_{5}$ | $+3 \cdot 8$ | -0.059 |
| Ethyl | $-0.572{ }^{\text {* }}$ | +16.0* | -0.188 | Decyl | -0.134 | $-6.0{ }_{2}$ | $-0.047_{5}$ |
| Propyl | $-0.313_{4}$ | $-8.3{ }_{6}$ | -0.137 | Dodecyl ......... | -0.1445 | $-0.11_{4}$ | $-0.036_{5}$ |
| Butyl | $-0.196_{1} \dagger$ | $-2 \cdot 0_{7} \dagger$ | -0.125 | Tetradecyl ...... | ca. 0 |  | $-0.025$ |
| Pentyl | $-0.226_{6}$ | $-5 \cdot 9$ | -0.090 | Hexadecyl | -0.0149 | $-2 \cdot 15$ | $-0.023_{5}$ |
| Hexyl | $-0.017_{5}$ | $-6 \cdot 6{ }_{1}$ | -0.078 | Octadecyl | ca. 0 | - | -0.023 |
| Heptyl | -0.1764 | $-2.2{ }_{6}$ | -0.072 | Cyclopentyl | $-0.230_{3}$ | $+1.24$ | -0.008 |
| Octyl | $-0.206_{3}$ | $-0.07_{6}$ | -0.065 | Cyclohexyl .... | $+0.322{ }_{7}$ | $-7 \cdot 3_{7}$ | $+0.012_{5}$ |

[^0]Table 3. Calculations of molar Kerr constants at infinite dilution in carbon tetrachloride at $25^{\circ}$.

| Solute alcohol | $\alpha \varepsilon_{1}$ | - $\beta$ | $\gamma$ | $\delta$ | $\infty\left({ }_{m} K_{2}\right) \times 10^{12}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Methyl | $17 \cdot 84$ | 1.096 | -0.165 | $-1.26$ | $-1.78$ |
| Ethyl | 12.54 | $1 \cdot 150$ | -0.129 | -8.18 | $-4 \cdot 08$ |
| Propyl | $9 \cdot 00$ | 1.061 | -0.094 | -4.48 | $-2 \cdot 96$ |
| Butyl | $7 \cdot 46$ | 1.025 | $-0.086$ | $-2 \cdot 80$ | $-2 \cdot 28$ |
| Pentyl | $6 \cdot 10$ | 0.983 | -0.062 | -3.24 | $-2 \cdot 6{ }_{9}$ |
| Hexyl | 5.55 | 0.964 | $-0.053_{5}$ | $-0.25$ | $-0 \cdot 6{ }_{6}$ |
| Heptyl | 4.90 | 0.981 | -0.049 | $-2.52$ | $-2 \cdot 4{ }_{4}$ |
| Octyl | $4 \cdot 28$ | 0.964 | $-0.045$ | -2.95 | $-2 \cdot 89$ |
| Nonyl | $3 \cdot 88{ }_{5}$ | 0.959 | -0.040 | $-5.61$ | $-6.0{ }_{6}$ |
| Decyl | $3 \cdot 64$ | 0.960 | $-0.033$ | $-1.92$ | $-1.95$ |
| Dodecyl | 2.97 | 0.935 | -0.025 | -2.06 | $-2 \cdot 1{ }_{0}$ |
| Tetradecyl | $2 \cdot 42$ | 0.924 | -0.017 | ca. 0 | $+1.2{ }_{3}$ |
| Hexadecyl | $2 \cdot 14$ | $0 \cdot 896$ | -0.016 | $-0.21$ | $+1 \cdot 2{ }_{5}$ |
| Octadecyl | 2.03 | 0.920 | -0.016 | ca. 0 | $+1.98$ |
| Cyclopentyl | 6.48 | 0.721 | $-0.005$ | $-3.29$ | $-2 \cdot 99$ |
| Cyclohexyl | 6.56 | 0.702 | $+0.009$ | $+4 \cdot 61$ | $+24 \cdot 1$ |

Table 4. Derivation of apparent polarisability semi-axes for the normal alcohols $\mathrm{C}_{1}$ io $\mathrm{C}_{6}$.

|  | $10^{35}$ | ${ }_{\mathrm{E}}{ }^{\text {P }}$ | $10^{23}$ | $10^{3}$ |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Alcohol | $\left(\theta_{1}+\theta_{2}\right)$ | (c.c.) | $\left(b_{1}+b_{2}+b_{3}\right)$ | $\infty \delta_{2}{ }^{2}$ | $10^{35} \partial_{1}$ | $10^{33} \theta_{2}$ | $\mu$ (D) | $10^{23} b_{1}$ | $10^{23} b_{2}$ | $10^{23} b_{3}$ |
| Methyl | $-0.423{ }_{3}$ | 8.04 | 0.956 | 12.05 | $0 \cdot 063{ }_{8}$ | $-0.487_{1}$ | 1.77 | 0.315 | $0 \cdot 363$ | 0.278 |
| Ethyl.. | $-0.970_{2}$ | $12 \cdot 62$ | 1.501 | $10 \cdot 0$ | $0 \cdot 131{ }_{6}$ | -1.102 | 1.79 | 0.492 | 0.566 | 0.444 |
| Propyl | $-0.7039$ | $17 \cdot 16$ | $2 \cdot 040_{5}$ | $9 \cdot 1{ }_{6}$ | $0 \cdot 220{ }_{8}$ | $-0.924_{7}$ | $1.73{ }_{5}$ | 0.672 | $0.763_{5}$ | 0.605 |
| Butyl.. | $-0.542$ | $21 \cdot 67$ | 2.577 | $8 \cdot 4$ | $0 \cdot 325{ }_{8}$ | $-0.868{ }_{0}$ | 1.75 | 0.852 | 0.959 | 0.766 |
| Pentyl | $-0.639_{7}$ | $26 \cdot 26$ | 3-123 | $7 \cdot 19$ | $0 \cdot 406{ }_{3}$ | $-1.046$ | $1.72_{5}$ | 1.032 | $1 \cdot 153$ | 0.938 |
| Hexyl | $-0.1569$ | $30 \cdot 72$ | $3 \cdot 653$ | $6.7{ }_{6}$ | $0.522^{8}$ | $-0.679_{7}$ | 1.77 | 1.212 | $1 \cdot 343$ | 1.098 |

how the values of $\delta_{\infty}{ }^{2}$ now obtained from solutions compare with others recorded earlier in the literature for liquid or gaseous alcohols, and (c) what indications, if any, do the present measurements give regarding the configurations adopted by alcohols as solutes. Comments will be made on these questions in the following paragraphs.
(a) The $\mathrm{O}-\mathrm{H}$ Bond Ellipsoid.-Unfortunately, from first principles, neither the direction of action of the resultant dipole moment within the reference system provided by the axes of the molecular polarisability ellipsoid, nor the desposition of those axes within the molecular framework, can be forecast with certainty. Possibly with the simplest case, that of methyl alcohol, there is a partial exception to this: the least of the polarisability axes may perhaps be identified as that which is perpendicular to the plane defined by the $\mathrm{C}-\mathrm{O}-\mathrm{H}$ chain.

If this is so, then an estimate of $b_{\mathrm{T}}{ }^{\mathrm{O}-\mathrm{H}}$ can be made straight away, provided $b_{\mathrm{T}}{ }^{\mathrm{C}-\mathrm{O}}$ and $b_{\mathrm{T}}{ }^{\mathrm{C}-\mathrm{H}}$ are known; these are thought ${ }^{7}$ to be $0.039 \times 10^{-23}$ and $0.063_{5} \times 10^{-23}$ respectively. The desired $b_{\mathrm{T}}{ }^{0-\text { II }}$ therefore appears as $\left(0.278-3 \times 0.063_{5}-0.039\right) \times 10^{-23}=0.049 \times$ $10^{-23}$. From the refractivity data given by Vogel et al. ${ }^{8}$ it appears that $R_{\infty}$ for the $\mathrm{O}-\mathrm{H}$ link is ca. 1.62 c.c., whence $b_{\mathrm{L}}{ }^{\mathrm{O}-\mathrm{H}}+2 b_{\mathrm{T}}{ }^{\mathrm{O}-\mathrm{H}}=0.193 \times 10^{-23}$; accordingly $b_{\mathrm{L}}{ }^{\mathrm{O}-\mathrm{H}}$ is obtained as $(0.193-0.098) \times 10^{-23}=0.095 \times 10^{-23}$. These estimates of the longtitudinal and transverse polarisabilities of the $\mathrm{O}-\mathrm{H}$ bond are advanced only provisionally. Clearly, they depend inter alia very much on the accuracy of the values taken for $b_{T}{ }^{\mathrm{O}-\mathrm{H}}$ and $b_{\mathrm{T}}{ }^{\mathrm{C}-\mathrm{O}}$. A final statement must await completion of work (by other authors) now proceeding on various hydroxyl-containing structures and ethers.

It is noted that Le Fèvre's empirical equation ${ }^{9}$ gives, with $r_{0-\mathrm{H}}=0.957 \AA$ (as in water) and $r_{\mathrm{H}}=0.375 \AA$ (from $r_{\mathrm{H}-\mathrm{H}}=0.75 \AA$; these $r^{\prime}$ 's are quoted from Tables compiled by Walsh ${ }^{10}$ ), a forecast that $10^{23} b_{\mathrm{L}} \mathrm{O}-\mathrm{H}$ is between 0.051 and 0.055 , and consequentially that $10^{23} b_{\mathrm{T}} \mathrm{O}-\mathrm{H}$ should be between 0.071 and 0.069 .

The contrast between these " predicted " values and those " found " is marked. The

[^1]origin of this may well be in Le Fèvre's equation which, to produce $b_{\mathrm{L}}{ }^{0-\mathrm{H}}=0.095 \times 10^{-23}$, requires $r_{\text {H }}$ to have the unexpected magnitude of $0.77 \AA$.

Certain indirect evidence may possibly be obtained from the case of the water molecule. It is known ${ }^{11}$ that $10^{3} \delta^{2}$ is around $34 \cdot 2$ for steam and $9 \cdot 8$ for liquid water (see Tables on pp. 54 and 84 of Bhagavantam ${ }^{11}$ ). Table 5 shows the values of molecular semi-axes, $10^{3} \delta^{2}$, etc., to be expected for $\mathrm{H}_{2} \mathrm{O}$ with an $\mathrm{H}-\mathrm{O}-\mathrm{H}$ angle of $105^{\circ}$ provided that this structure may be regarded from the polarisability viewpoint as simply composed of two $\mathrm{O}-\mathrm{H}$ bond ellipsoids. Attention is naturally attracted to the first line of Table 5 in which is shown a (probably fortuitous) congruence with the recorded $\Delta^{2}$ vapour of steam. It is plain that the $\mathrm{O}-\mathrm{H}$ link

Table 5. The molecular anisotropy of $\mathrm{H}_{2} \mathrm{O}$ expected for different values of $b_{\mathrm{L}}{ }^{\mathrm{OH}}$ and $b_{\mathrm{T}}{ }^{\mathrm{OH}}$.

| $b_{\mathrm{L}} \mathrm{O}-\mathrm{H}$ | $b_{\mathrm{T}} \mathrm{O}-\mathrm{H}$ | $b_{1} \mathrm{H}_{2} \mathrm{O}$ | $b_{2} \mathrm{H}_{2} \mathrm{O}$ | $b_{3} \mathrm{H}_{2} \mathrm{O}$ | $10^{3} \delta_{\text {caic. }}$ | $\left(2 b_{1}-b_{2}-b_{3}\right)$ |
| :--- | :--- | :--- | :--- | :--- | :---: | :---: |
| 0.095 | 0.049 | 0.132 | 0.156 | 0.098 | 34.2 | +0.010 |
| $0.0644_{3}$ | $0.064_{3}$ | 0.129 | 0.129 | 0.129 | 0 | 0 |
| 0.055 | 0.069 | 0.128 | 0.120 | 0.138 | 3.3 | -0.002 |
| 0.051 | 0.071 | 0.127 | 0.117 | 0.142 | 6.4 | -0.005 |
| 0.041 | 0.076 | 0.126 | 0.108 | 0.152 | 19.7 | -0.008 |

cannot be isotropic, otherwise $\delta^{2}{ }_{H_{2} \mathrm{O}}$ would be zero. If, however, the ratio $b_{\mathrm{L}} \mathrm{O}-\mathrm{I} / b_{\mathrm{T}} \mathrm{O}-\mathrm{H}$ were less than unity a finite $\delta^{2} \mathrm{H}_{2} \mathrm{O}$ should also appear, accompanied by a negativity in $2 b_{1}-b_{2}-$ $b_{3}$. For instance, with $b_{\mathrm{L}}{ }^{0-\mathrm{H}}=0.051 \times 10^{-23}$ and $b_{\mathrm{T}}{ }^{\mathrm{O}-\mathrm{H}}=0.071 \times 10^{-23}$, we obtain $\theta_{1}=0.005 \times 10^{-35}$ and $\theta_{2}=-0.21 \times 10^{-35}$ (with $\mu_{\mathrm{H}_{2} \mathrm{O}}=1.8 \mathrm{D}$ ), so that ${ }_{\mathrm{m}} K_{\mathrm{H}_{2} \mathrm{O}}$ should be negative. Neither the molar Kerr constants of water nor of steam are yet on record, although early observations by Schmidt ${ }^{12}$ and Pauthenier ${ }^{13}$ suggest that water in bulk displays positive electric birefringence. (Owing to the highly associated and hydrogenbonded state of water, the last fact may be irrelevant.)
(b) Literature Values of $\delta^{2}$ for Alcohols.-In the main, the light-scattering data concerned have been provided by Krishnan, ${ }^{14}$ Ramakrishna Rao, ${ }^{15}$ and Peyrot; ${ }^{16}$ the results of, and references to, these and other workers are included in the books of Cabannes ${ }^{17}$ and Bhagavantam. ${ }^{11}$ Table 6 compares earlier measurements of $10^{3} \delta^{2}$, made on the alcohols as liquids and gases, with those now obtained at infinite dilution in carbon tetrachloride. (To put the literature values of $\delta^{2}$ on the same numerical basis as $\infty \delta_{2}{ }^{2}$ they have been doubled.)

Table 6. Past and present values of $10^{3} \delta^{2}$ for the first six $n$-alcohols.

|  | State in which measured: | As liquid | As vapour | As liquid | As vapour | At infinite dilution in $\mathrm{CCl}_{4}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Alcohol |  | (a) | (b) | (c) | (d) | (e) |
| Methyl |  | $7 \cdot 8$ | $28 \cdot 6$ | $7 \cdot 0$ | $29 \cdot 0$ | $12 \cdot 0_{5}$ |
| Ethyl | . | $4 \cdot 4$ | $15 \cdot 4$ | $5 \cdot 2$ | $15 \cdot 2$ | $10 \cdot 1$ |
| Propyl |  | $3 \cdot 0$ | $23 \cdot 0$ | $3 \cdot 8$ | $20 \cdot 2$ | $9 \cdot 1_{6}$ |
| Butyl |  | $4 \cdot 2$ | $27 \cdot 6$ | $3 \cdot 2$ | $29 \cdot 0$ | $8 \cdot 4{ }_{7}$ |
| Pentyl |  | $4 \cdot 66$ | $20 \cdot 2$ | $3 \cdot 0$ | $22 \cdot 0$ | $7 \cdot 19$ |
| Hexyl |  | - | - | - | - | 6.76 |

(Values in columns $a$ and $b$, due to Krishnan and R. Rao respectively, are from Cabannes, ref. 17, pp. 252, 253; those in $c$ and $d$, due to various authors, are from Bhagavantam, ref. 11, pp. 55 and 84 ; those in $e$ are from ref. 3).
$\infty_{\infty} \delta_{2}{ }^{2}$ diminishes with the addition of each extra $\mathrm{CH}_{2}$ group, implying that the larger the solute molecule the less its anisotropy. A parallel tendency is displayed, at a generally lower level of anisotropy, among the values for $\delta^{2}$ liquid. Because of the association known
${ }_{12}$ Bhagavantam, "Scattering of Light and the Raman Effect," Andhra Univ., Waltair, 1940.
12 Schmidt, Diss., Göttingen, 1901.
${ }^{13}$ Pauthenier, Compt. vend., 1921, 172, 383.
14 Krishnan, Phil. Mag., 1925, 50, 697.
${ }^{15}$ Ramakrishna Rao, Ind. J. Physics, 1927, 2, 61.
16 Peyrot, Compt. vend., 1936, 203, 1512.
${ }^{17}$ Cabannes, "La Diffusion Moléculaire de la Lumière," Les Presses Universitaires de France, Paris, 1929.
to occur with pure alcohols, and the large number of possible configurations of hydrogenbonded "polymeric" species contained in their liquid phases, $\delta^{2}$ liquid is not a property which can easily or usefully be analysed. Yet it is surprising that $\delta^{2}$ liquid should appear more regularly comparable with $\infty_{2}{ }_{2}{ }^{2}$ than with $\delta^{2}$ vapour, since it is believed that both at infinite dilution and in the gaseous state the individual alcohol molecules are separate. The measurements from which the values of $\infty_{\infty} \delta_{2}{ }^{2}$ have been drawn were deliberately made in concentration regions thought (from dielectric polarisation data) to be low enough to avoid the intervention of association effects. In any case, with the techniques available, observations of the $\Delta$ 's of still more dilute solutions were not possible with any dependable accuracy. It is perhaps a coincidence, but worth mentioning, that ethyl alcohol with the smallest $\delta^{2}$ vapour shows the largest negative molar Kerr constant at infinite dilution; one may suspect therefore that the root of the problem is not the separateness of the molecules, but rather their configurations, which differ in gas and solution. A study of the values of ${ }_{\mathrm{m}} K$ of alcohols as vapours would provide pertinent information.
(c) The Configurations of Alcohols as Solutes.-As already stated, the molecular semiaxes of the alcohols named in Table 4 have been computed as though the resultant dipole moments act along one of the principal axial directions. Using the " provisional " values $10^{23} b_{\mathrm{L}}{ }^{\mathrm{OH}}=0 \cdot 10$ and $10^{23} b_{\mathrm{T}} \mathrm{OH}=0.05$, we can perform the following calculations for methyl alcohol. The oxygen valency angles in $\mathrm{H}_{2} \mathrm{O}$ and $\mathrm{Me}_{2} \mathrm{O}$ are $105^{\circ}$ and $111^{\circ}$ respectively, ${ }^{10}$ whence component bond moments follow as $\mu_{\mathrm{OH}}=1 \cdot 5 \mathrm{D}$ and $\mu_{\mathrm{O}-\mathrm{o}}=1 \cdot \mathrm{ID}_{\mathrm{D}}$. In MeOH these may be taken as interacting at $108^{\circ}$, producing a resultant of $1 \cdot 77 \mathrm{D}$. This resultant is therefore disposed at just over $60^{\circ}$ to the $\mathrm{C}-\mathrm{O}$ line. Accordingly, the polarisabilities to be expected collinearly with and perpendicularly to $\mu_{\text {resultant }}$ are:

$$
\begin{aligned}
& 10^{23} b_{1}=0.192+0.081 \cos ^{2} 60+0.039 \sin ^{2} 60+0.10 \cos ^{2} 48+0.05 \sin ^{2} 48 \\
& 10^{23} b_{2}=0.192+0.081 \cos ^{2} 30+0.039 \sin ^{2} 30+0.10 \cos ^{2} 42+0.05 \sin ^{2} 42 \\
& 10^{23} b_{3}=0.192+0.039+0.05
\end{aligned}
$$

The results are in reasonable agreement with the magnitudes found:

$$
\begin{array}{crrrrrrrrr} 
& & \text { Calc. } & \text { Found } & & & \text { Calc. } & \text { Found } & & \\
10^{23} b_{1} & \ldots & 0 \cdot 31_{4} & 0.31_{5} & 10^{23} b_{2} \ldots & 0 \cdot 34_{0} & 0 \cdot 36_{3} & 10^{23} b_{3} \ldots & 0 \cdot 28_{1} & 0 \cdot 27_{8}
\end{array}
$$

With the next homologue, ethyl alcohol, an infinitude of configurations between s-cis and $s$-trans is theoretically possible, although (for steric reasons) structures near the $s$-cis extreme would seem less likely than those in which the $\mathrm{CH}_{3}$ group and the H atom are farther apart. For the s-trans extreme form of ethyl alcohol $b_{3}$ should be:

$$
5 b_{\mathrm{i}}^{\mathrm{OH}}+b_{\mathrm{T}}^{\mathrm{C}-\mathrm{O}}+b_{\mathrm{T}}^{\mathrm{C}-\mathrm{O}}+b_{\mathrm{T}}^{\mathrm{O}-\mathrm{H}}=0.436 \times 10^{-23}
$$

For the form intermediate between s-cis and s-trans (in which the triangles defined by $\mathrm{CH}_{3}-\mathrm{C}-\mathrm{O}$ and $\mathrm{H}-\mathrm{O}-\mathrm{C}$ are in perpendicular planes) $b_{3}$ should be:

$$
5 b_{\mathrm{i}}{ }^{\mathrm{CH}}+b_{\mathrm{T}}{ }^{\mathrm{C}-\mathrm{O}}+b_{\mathrm{T}}{ }^{\mathrm{O}-\mathrm{H}}+0.0986 \cos ^{2} 20+0.0274 \sin ^{2} 20=0.499 \times 10^{-23}
$$

The values observed is $b_{3}=0.444 \times 10^{-23}$ with which the first prediction fits better than the second. Estimates of $b_{1}$ and $b_{2}$ for the s-trans configuration are also in fair agreement with experiment:

$$
\begin{array}{ccccccccccc} 
& & \text { Calc. } & \text { Found } & & & \text { Calc. } & \text { Found } & & & \text { Calc. }
\end{array} \text { Found }
$$

Empirical calculations of the potential barriers to internal rotation, made several years ago by Aston et al., ${ }^{18}$ showing the trans-form to be stabler than the cis by ca. $1500 \mathrm{cal} . / \mathrm{mole}$, are consistent with our conclusion.

Inspection of the semi-axes listed in Table 4 reveals that there is a rough equality in the increase of $b_{1}, b_{2}$, and $b_{3}$ per additional $\mathrm{CH}_{2}$ group. If $\Delta b_{i}$ is the change from one

[^2]alcohol to its next, higher homologue, then the "apparent" $b_{\mathrm{i}}$ 's (listed before) show differences as follows:

| $\Delta b_{1}$ | $0 \cdot 177$ | $0 \cdot 180$ | $0 \cdot 180$ | $0 \cdot 180$ | $0 \cdot 180$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\Delta b_{2}$ | $0 \cdot 203$ | $0 \cdot 197{ }_{5}$ | $0 \cdot 195_{5}$ | 0-194 | $0 \cdot 190$ |
| $\Delta b_{3}$ | $0 \cdot 166$ | $0 \cdot 161$ | $0 \cdot 161$ | 0.172 | $0 \cdot 160$ |

These differences are close to those seen between the calculated values for ethyl and methyl alcohols, viz.,

$$
0.497-0.314=0.183 ; 0.537-0.340=0.197 ; 0.436-0.281=0.155
$$

a fact which suggests a certain repetitive commonness of configuration among the six alcohols under consideration. In particular, it is interesting that in ascending the series stage by stage by the addition of one $\mathrm{C}-\mathrm{C}$ and two $\mathrm{C}-\mathrm{H}$ links to each previous alcohol, it appears that the ellipsoid of the entrant C-C link is constantly inclined to the $b_{1}, b_{2}$, and $b_{3}$ directions in each previous alcohol. Indeed, it seems that this constant inclination cannot be far from half the tetrahedral angle $(T / 2)$ or $180^{\circ}-T / 2$, i.e.,

$$
\Delta b_{\mathrm{i}}=2 b_{\mathrm{i}}^{\mathrm{CH}}+0.0986 \cos ^{2}(T / 2)+0.0274 \sin ^{2}(T / 2)=0.179 \times 10^{-23}
$$

This is almost exactly the $\Delta b$ noted above for the $b_{1}$ direction, and is close to the mean of all the $\Delta b$ 's taken together.

Nothing is here disclosed which is out of harmony with the accepted ideas of carbon stereochemistry: the normal alcohols may have their alkyl chains as near-flat zig-zags or arranged along helical paths. That the latter possibility deserves serious consideration is obvious from the arguments of Mumford ${ }^{19}$ which, although stated primarily for the homologous $n$-aliphatic hydrocarbons, are of course easily transferable to any series having $\mathrm{C}_{n} \mathrm{H}_{2 n+1}$ groups. An extension of the present study (of Kerr effects, depolarisation factors, etc.) to bridge Mumford's $\mathrm{C}_{16}$ discontinuity would be worth while.

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19 Mumford, $J ., 1952,4897$.


[^0]:    * Computed from solutions having values of $w_{2}$ between 0.01661 and zero.
    $\dagger$ Ditto, between 0.02288 and zero.

[^1]:    7 Le Fèvre and Le Fèvre, $J ., 1956,3549$.
    ${ }^{8}$ Vogel, Cresswell, Jeffrey, and Leicester, J., 1952, 514.
    ${ }^{9}$ Le Fèvre, Proc. Chem. Soc., 1958, 283.
    ${ }^{10}$ Walsh, " Progress in Stereochemistry," Ed. Klyne, Vol. 1, Butterworths, London, 1954, Chap. I.

[^2]:    ${ }^{18}$ Aston, Isserow, Szasz, and Kennedy, J. Chem. Phys., 1944, 12, 336; Brickwedde, Moskow, and Aston, J. Res. Nat. Bur. Stand., 1946, 37, 263; cf. also J. Chem. Phys., 1943, 11, 532; 1949, 17 , 111.

